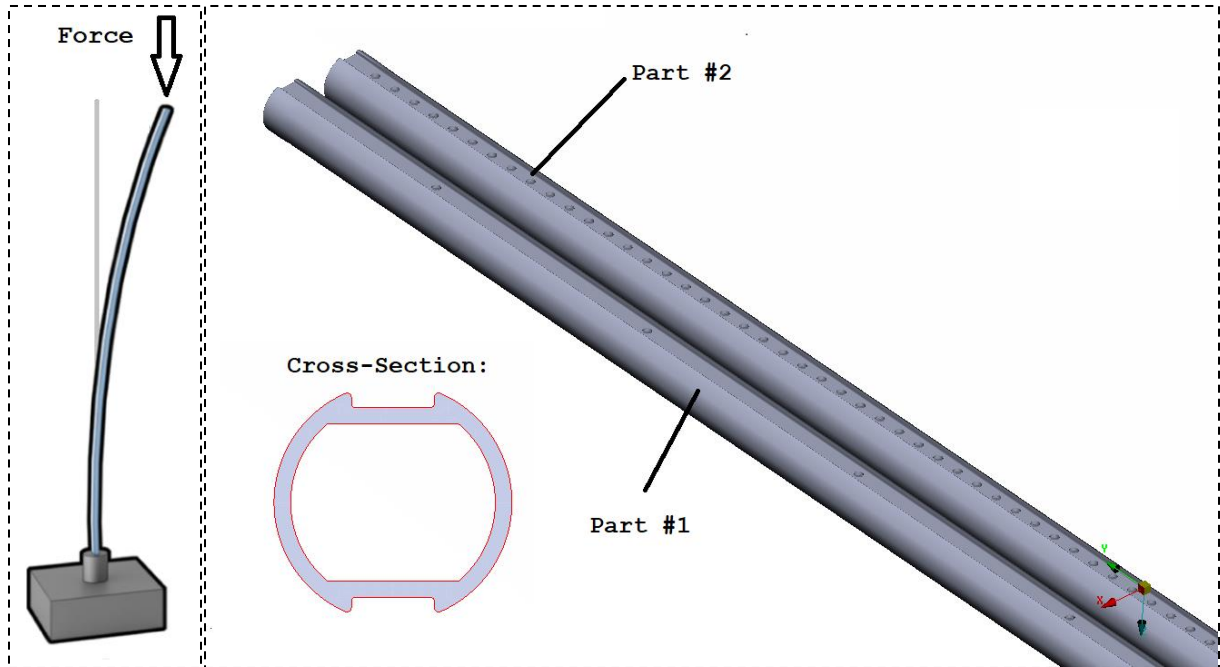


## Aluminum poles - Buckling analysis report

Objective of the analysis: to find out numerically critical strength of aluminum poles with boundary conditions shown on Picture 1.



[Picture 1] Boundary conditions of numerical experiment and overall view on the poles.

Several Methods were used for analysis:

- Analytical estimation (Euler buckling + local buckling)
- Linear buckling (NASTRAN SOL105)
- Non-linear buckling (NASTRAN SOL106 with LGDISP)

## 1. Analytical Estimation

### Overall buckling

Input data:  $E := 68.9 \text{ GPa}$      $A := 177 \text{ mm}^2$      $k_{Holes\_Pole\_2} := 0.038$   
 $L := 2372 \text{ mm}$      $J_1 := 12715 \text{ mm}^4$   
 $\mu := 2$      $J_2 := 15040 \text{ mm}^4$



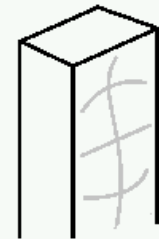
Pole #1 (neglecting holes):  $P_{Euler\_Pole\_1} := \frac{\pi^2 \cdot E}{(\mu \cdot L)^2} \cdot J_1 = 384 \text{ N}$      $\sigma_{Euler} := \frac{P_{Euler\_Pole\_1}}{A} = 2.17 \text{ MPa}$

Pole #2 (estimating holes):  $P_{Euler\_Pole\_2} := \frac{\pi^2 \cdot (E \cdot (1 - k_{Holes\_Pole\_2}))}{(\mu \cdot L)^2} \cdot (J_1 \cdot (1 - k_{Holes\_Pole\_2})) = 356 \text{ N}$

### Local buckling: estimation of weaker (planar) side

Extra Input data:  $\delta := 2 \text{ mm}$      $k_{Boundary} := 3.6$   
 $b := 15 \text{ mm}$

$$k_{Holes\_on\_Side} := \frac{168 \cdot \frac{\pi \cdot (5 \text{ mm})^2}{4}}{L \cdot b} = 0.093$$



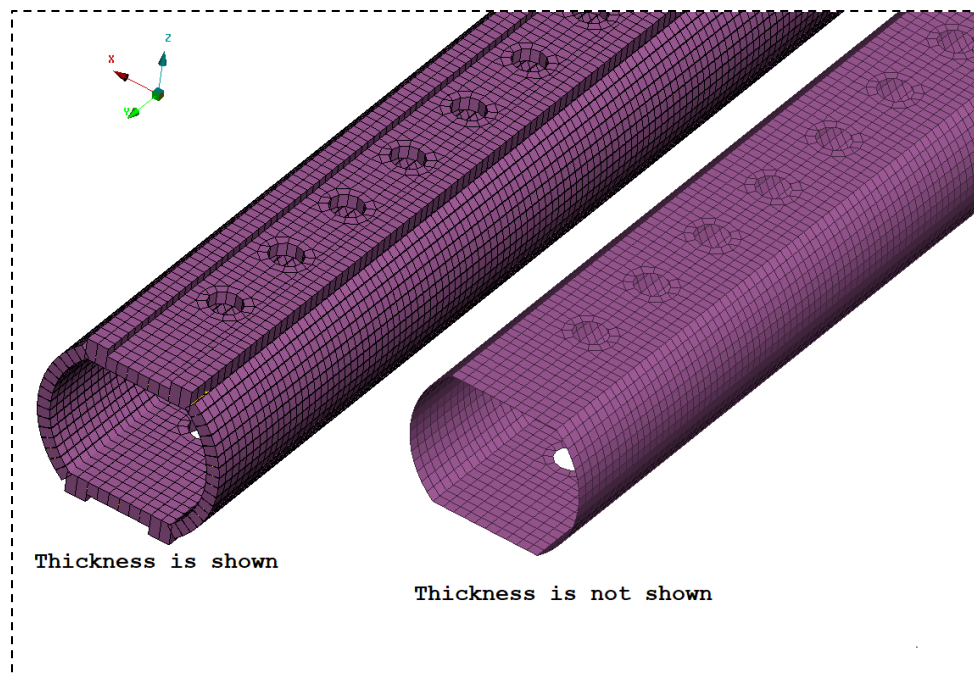
Critical force:  $P := \frac{k_{Boundary} \cdot E}{\left(\frac{b}{\delta}\right)^2} \cdot (b \cdot \delta) \cdot (1 - k_{Holes\_on\_Side})^3 = 98800 \text{ N}$

Key points from analytical calculation:

- Expected critical load for **Pole #1 = 384 N**, for **Pole #2 = 356 N**
- Critical stress is in aluminum linear zone ( $\sigma_{Euler} \ll \sigma_{Yield\_Al\_6061}$ )
- Local buckling is of no interest, since  $P_{Local} \gg P_{Overall}$

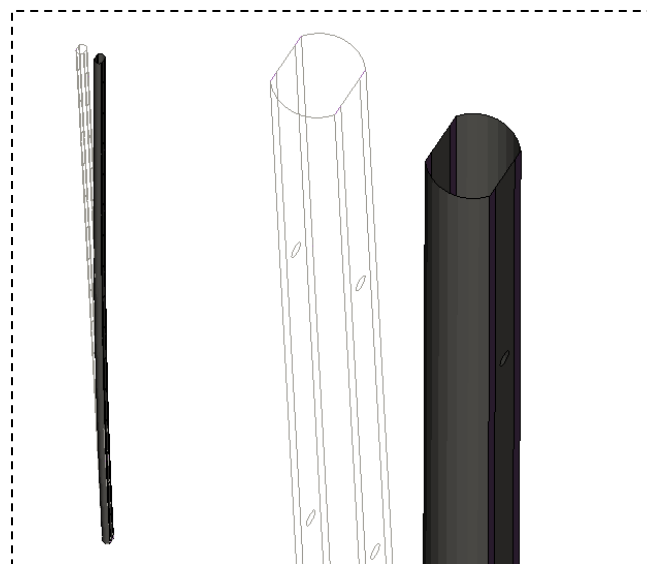
## 2. Numerical linear buckling

Finite-element model used for both linear and non-linear analysis is shown on Picture 2. Nastran CQUAD4 and CTRIA3 elements are used. CQUADs are used with offset and variable thickness.



[Picture 2] Finite element model of Pole #2.

First buckling form is identical to Pole #1 and Pole #2 and is shown on Picture 3.



[Picture 3] First buckling form of Pole #1.

Resulting critical forces are:

For Pole #1 = **398 N**

For Pole #2 = **362 N**

### 3. Numerical non-linear buckling

Buckling in non-linear cases is analyzed with the help of StabilityPath. Since Poles have very simple structure, any nodes can be chosen for Stability Path, as shown on Pictures 4 and 5.

#### Results for Pole #1 are:

Pole #1 was analyzed with Load = 410 N.

Non-linear effects start at =  $0.9 \times 410 \text{ N} = 369 \text{ N}$

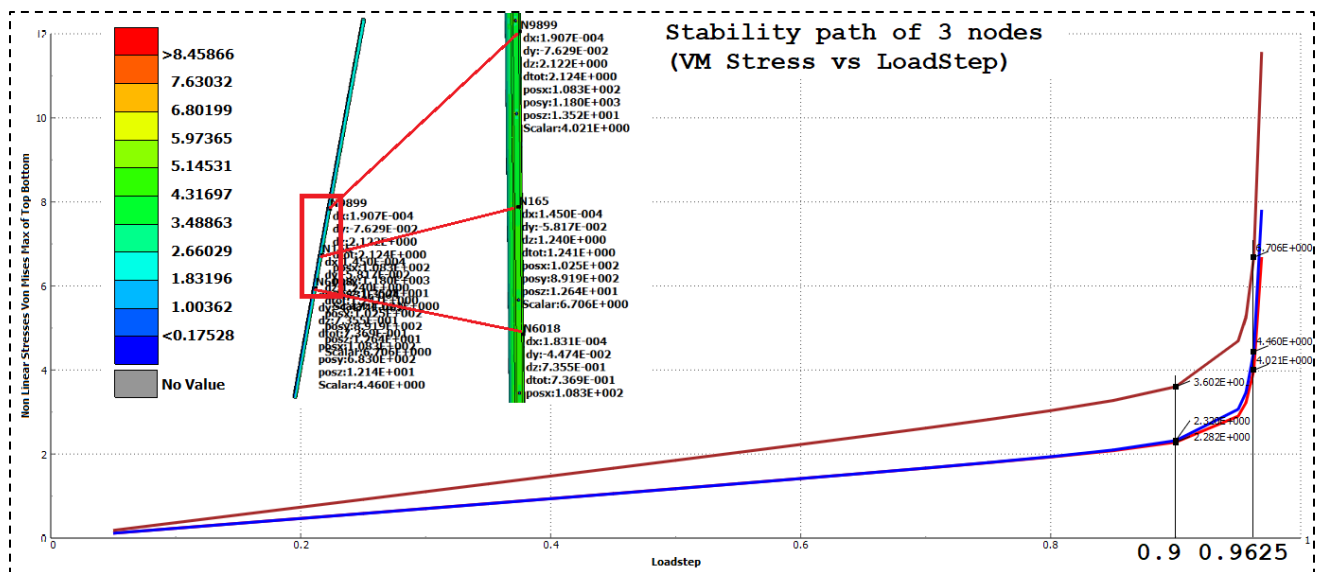
Stresses begin to raise exponentially (defining critical load) at =  $0.9625 \times 410 \text{ N} = 395 \text{ N}$

#### Results for Pole #2 are:

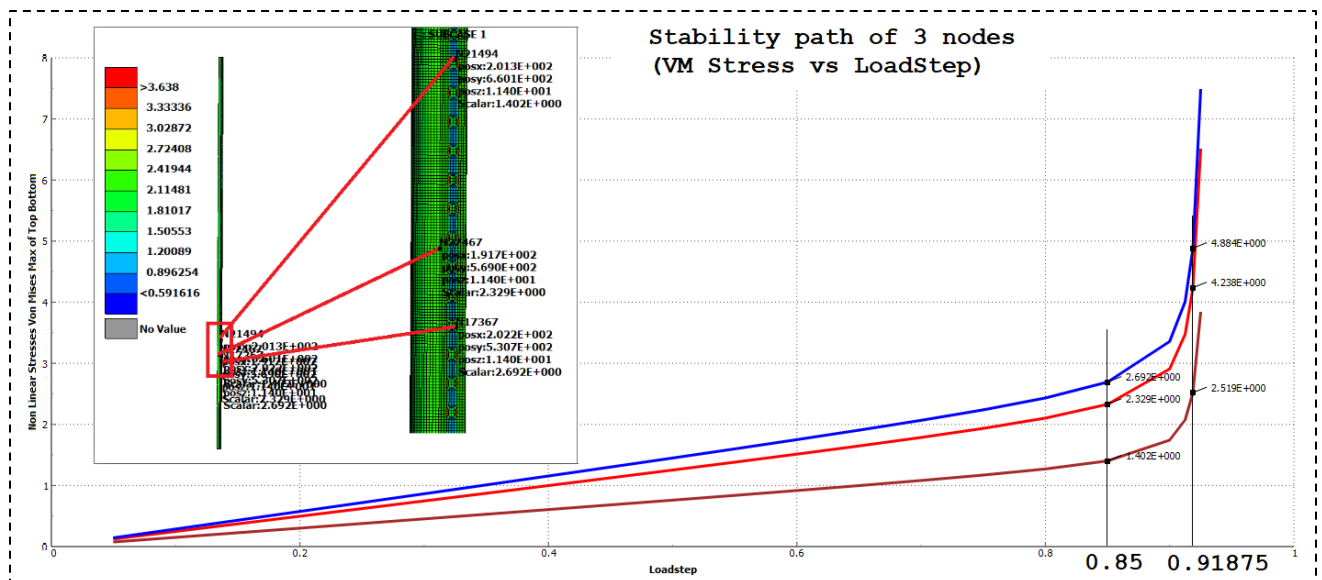
Pole #2 was analyzed with Load = 390 N.

Non-linear effects start at =  $0.85 \times 390 = 331.5 \text{ N}$

Stresses begin to raise exponentially (defining critical load) at =  $0.91875 \times 390 = 358 \text{ N}$



[Picture 4] Stability path for Pole #1 (100% load = 410 N).



[Picture 5] Stability path for Pole #2 (100% load = 390 N).

## 4. Conclusions

Summary of various critical force calculation methods is shown in the table:

	Analytical	Numerical Linear	Numerical Non-Linear
<b>Pole #1 Critical Force</b>	384 N	398 N	395 N
<b>Pole #2 Critical Force</b>	356 N	362 N	358 N

Final Results, bases on the safest method (analytical):

<b>Pole #1 Critical Force</b>	<b>384 N</b>
<b>Pole #2 Critical Force</b>	<b>356 N</b>

*Please, notice that **safety factor** should be considered on the top of Critical Force (based on industry standards) before assuming final permissible load!*

**Engineering center Frontier Machines**

Engineering stress analysis of any difficulty

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